

(2) When you put cream in your coffee, which causes the larger increase in entropy, the mixing of cream and water or the heat exchange between cream and water?

Let  $M$  be the mass of the coffee,  $m$  and  $c_v$  the mass and heat capacity of the cream. I shall adopt a temperature of  $273 + 57$ , or  $330^\circ \text{K}$  for the coffee, and  $273 + 17$ , or  $290^\circ \text{K}$  for the initial temperature of the cream. To the first order in  $m/M$  the entropy increase resulting from the heat exchange,  $\Delta S_{\text{heat}}$ , is  $m c_v (330 - 290)(1/310 - 1/330)$ , which is  $0.008 m c_v$ . For the mixing entropy increase,  $\Delta S_{\text{mix}}$ , we must disregard the water in cream. (Remember the Gibbs paradox!) Assume a fraction  $f$  of the cream is not water, but

is something else—presumably butterfat—with molecular weight  $W_{\text{cr}}$ . These molecules,  $fm/W_{\text{cr}}$  of a mole, are now distributed through a volume  $M/m$  times larger, so the mixing entropy change is  $(fm/W_{\text{cr}}) R \ln(M/m)$ . With  $R = 2 \text{ cal/mole deg}$ , and  $c = 1 \text{ cal/gm deg}$ , I'll assume  $f = 1/3$  and  $M/m = 10$ . The ratio  $\Delta S_{\text{mix}}/\Delta S_{\text{heat}}$  is then  $200/W_{\text{cr}}$ . The molecular weight of a "cream" molecule is surely greater than 200. A chemist friend thought 800 might be reasonable. So it appears that the heat exchange causes the larger increase in entropy—but not by a large factor.